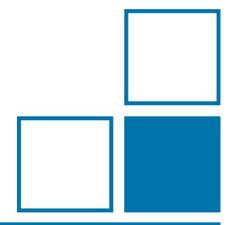


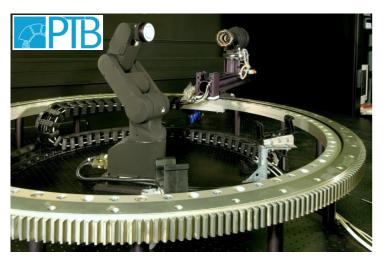


# Comparison of goniospectrophotometers

## Dr. Christian Strothkämper

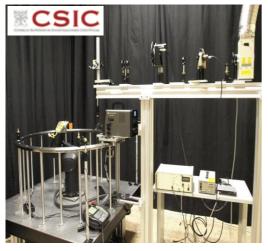
Physikalisch-Technische Bundesanstalt WG 4.24 "Reflection and Transmission" Bundesallee 100 38116 Braunschweig









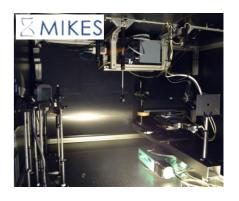


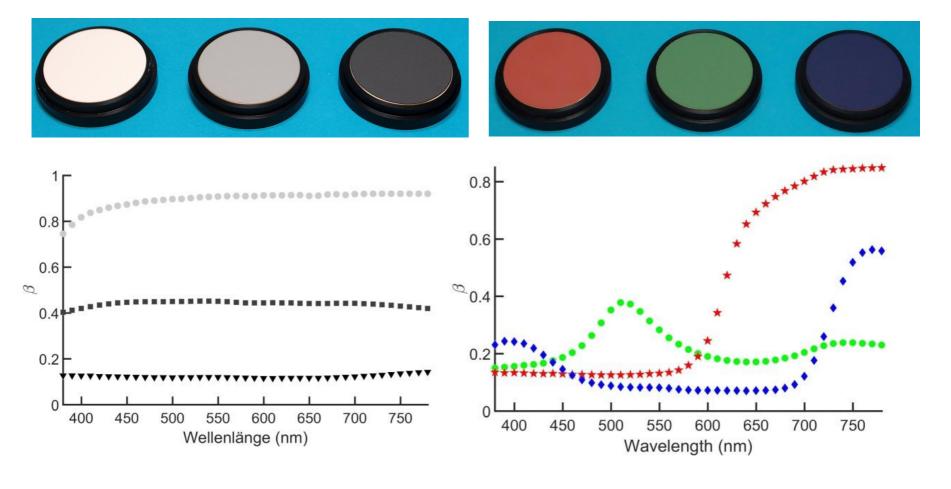










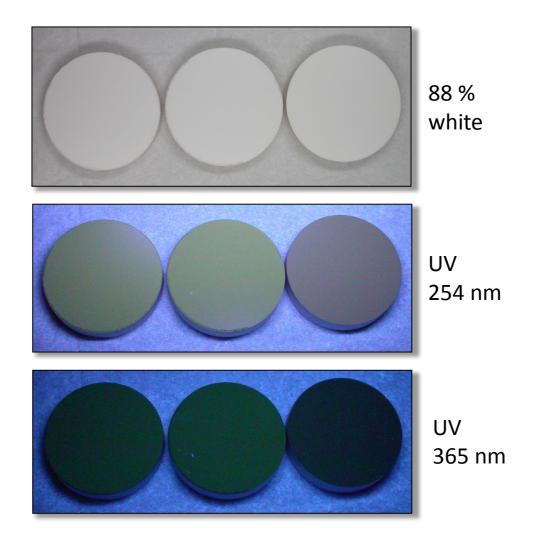


Objective: Test the scales for different magnitues and spectral variations of the BRDF in 0:45 (45:0) geometry.



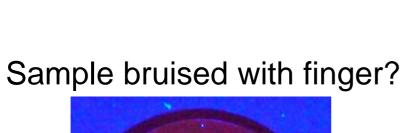
Precautions were taken for the distribution of the samples

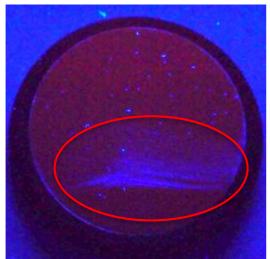
#### And they were routinely inspected

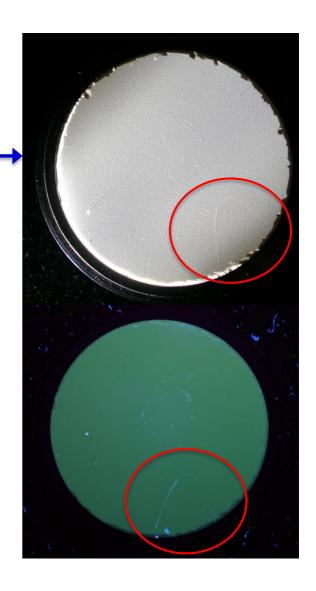




Improper Sample-Handling!







Each participant provides a  $\beta_n$  with uncertainty  $u_n$ 

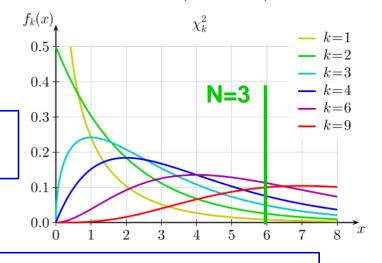
Calculate KCRV as weighted mean  $\beta = \frac{\sum_{n} w_n \beta_n}{\sum_{n} w_n}$  and ist uncertainty  $u = (\sum_{n} w_n)^{-1/2}$ 

Calculate 
$$\chi^2$$
 sum  $\chi^2 = \sum_n \frac{(\beta_n - \beta)^2}{u_n^2}$ 

Sum in the 95% quantile of the  $\chi^2$  distribution with N-1 degrees of freedom?

yes





 $\left(w_n = \frac{1}{u_n^2}\right)$ 

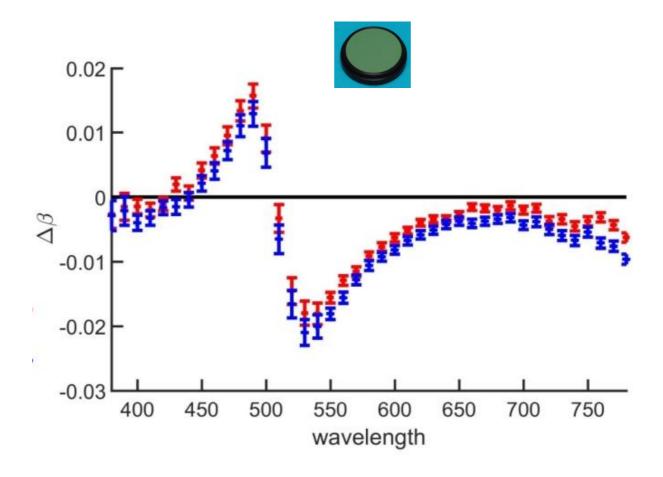
Calculate degree of equivalence  $(d_n, U(d_n))$  for each participant with

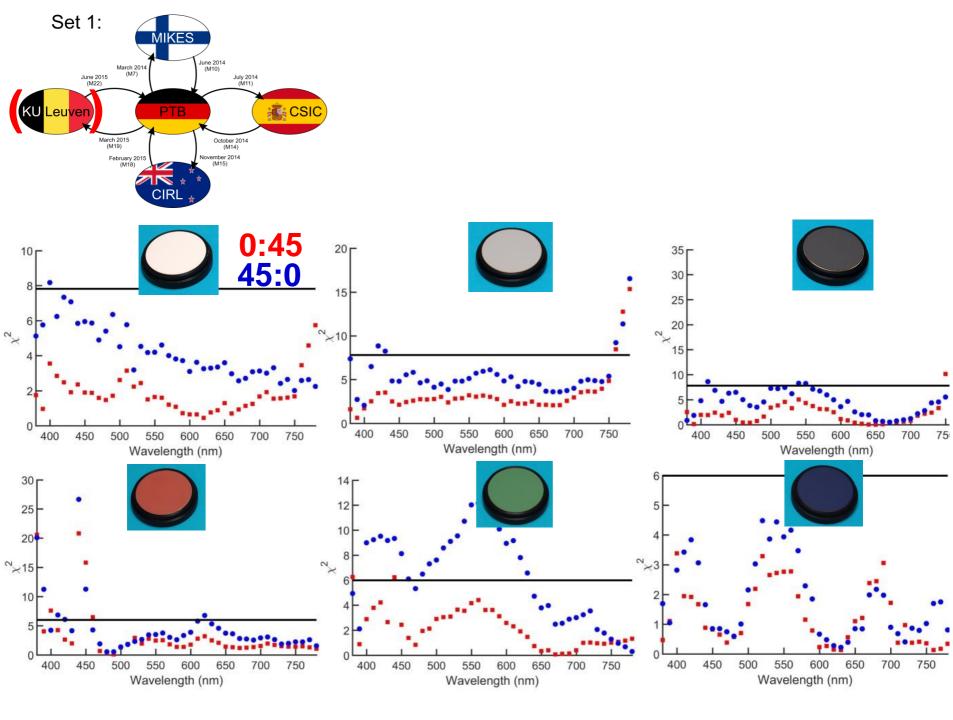
$$d_n = \beta_n - \beta$$
$$U(d_n) = 2\sqrt{u_n^2 - u^2}$$

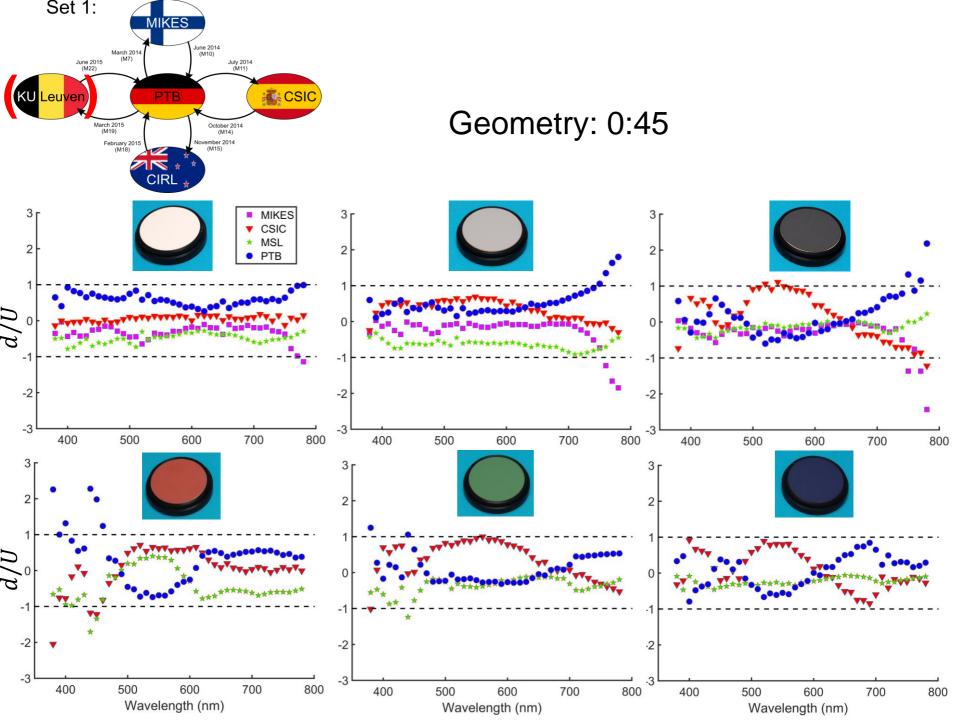
- Revise uncertainty budget
- Exclude participants
- Use more general data evaluation (e.g. median as the KCRV)

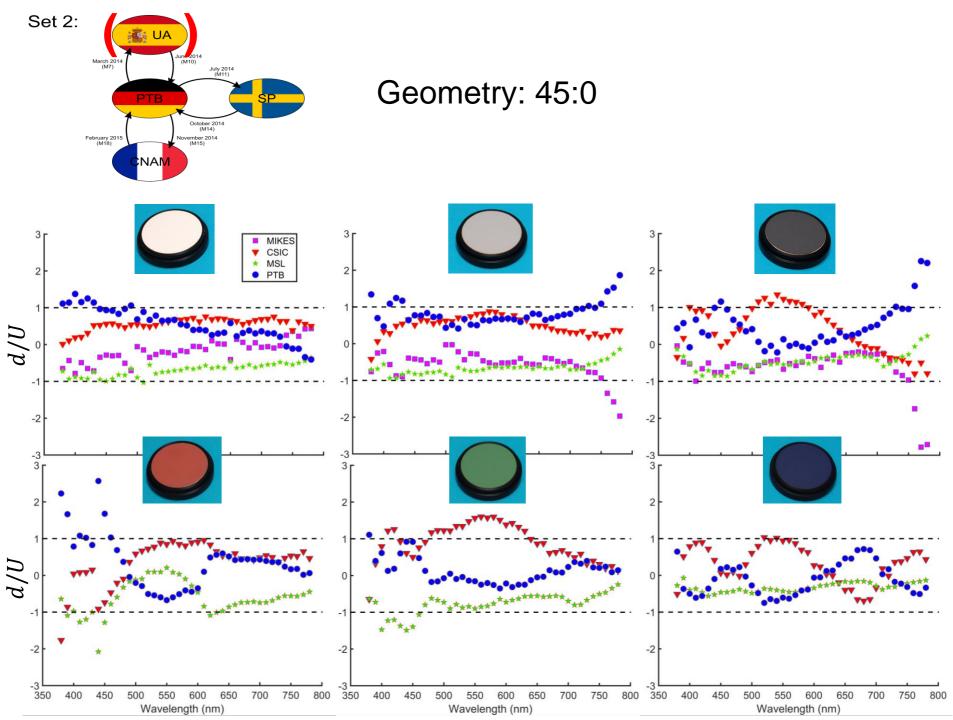
## Example where results don't fit

Deviation of KU Leuven to KCRV from PTB, MIKES, CSIC and MSL

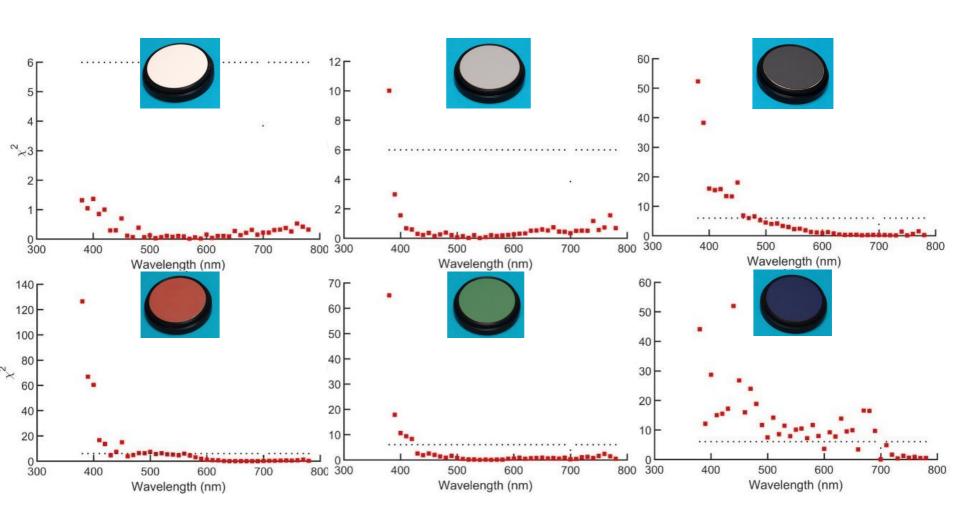


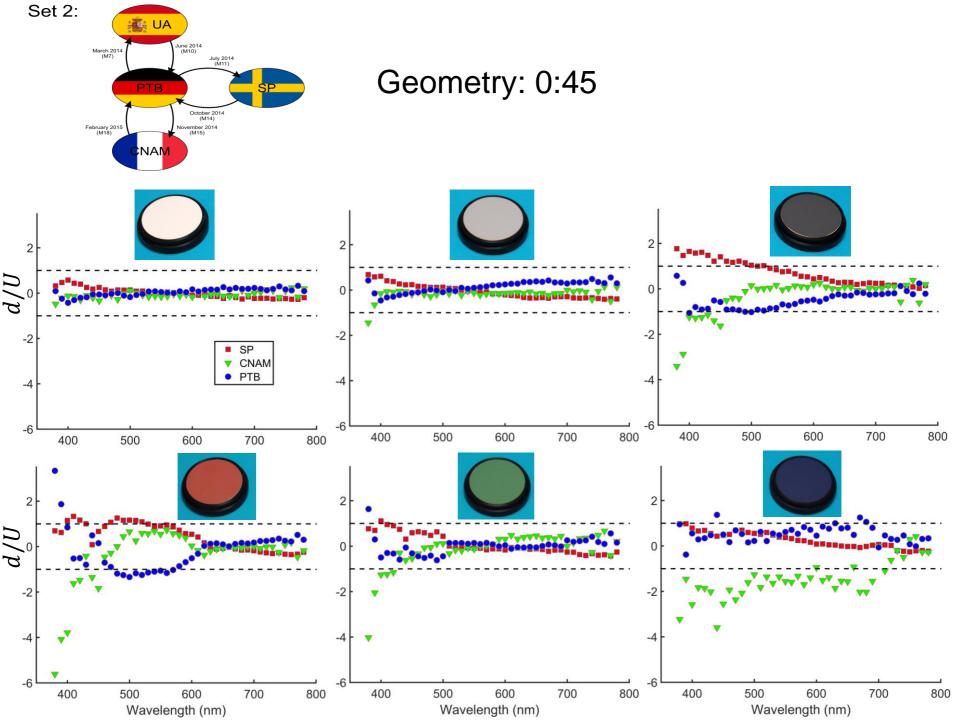




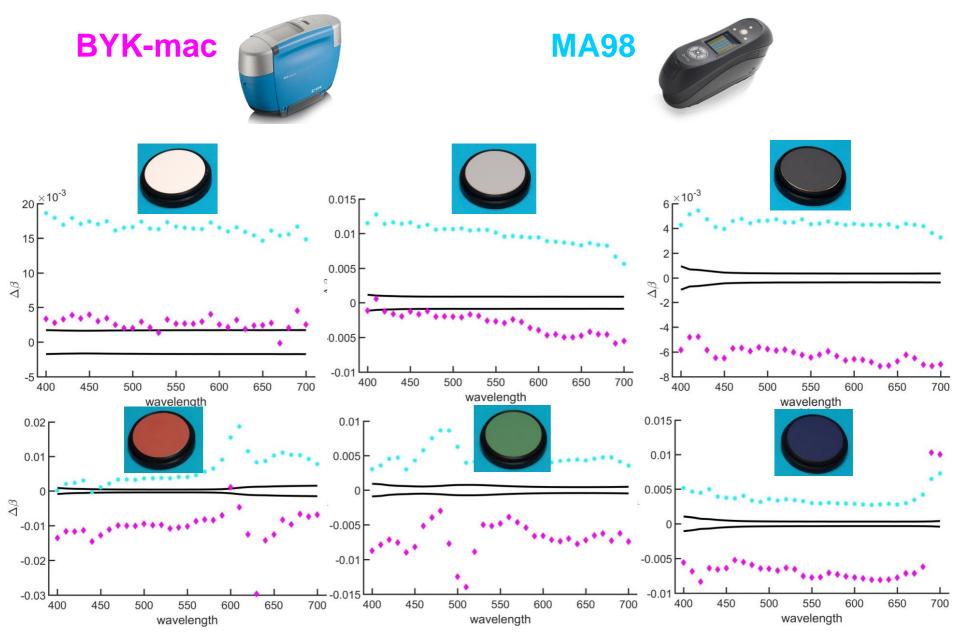


Geometry: 0:45





#### Deviation of the commercial instruments from the KCRV



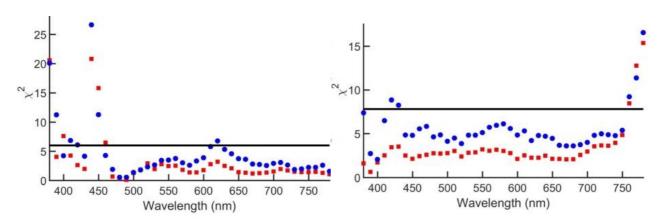
• The results are consistent and the scales of the involved NMIs agree in 0:45 and/or 45:0 geometry



 Commercial instruments haver larger uncertainties, respectively, deviate by a bigger margin from the NMI results.



 Extended scale comparison (wavelength, geometries) should be planned



 Of special interest are geometries with a very high polar angle for detection or illumination as they are particularly suitable to assess systematic effects

$$\beta \approx \frac{1}{\cos \theta}$$

### You'll have the opportunity to catch up more details

The quantity that is derived from the measurements and compared between the different instruments is the spectral -radiance factor (SRF):

$$\beta(\theta_{i}, \varphi_{i}; \neg \theta_{gr}, \varphi_{rg}; \neg \lambda) = \frac{L_{\mathbf{r}}(\theta_{i}, \varphi_{i}; \theta_{r}, \varphi_{r}; \lambda \theta_{s}, \varphi_{s}, \theta_{s}, \varphi_{s}, \lambda)}{L_{PRD}},$$
(1)

where  $L_{\rm r}$  denotes the radiance of a sample and  $L_{\rm PRD}$  is the radiance of the perfectly reflecting diffuseer (Lambertian reflection and therefore independent of the bidirectional geometry) under identical conditions of illumination. The BRDF on the other hand, is defined by the ratio of  $L_{\rm r}$  to the irradiance  $E_{\rm i}$  on the sample. The BRDF can be related with the SRF by relating this irradiance with the term  $L_{\rm PRD}$  in Eq. 1. Since As the radiance is independent of the geometry constant for the PRD, i.e.

$$L_{\text{PRD}} = \frac{\partial^2 \Phi I(\theta_r, \varphi_r \theta_{\overline{x}}, \varphi_{\overline{x}})}{\partial \Omega \partial A \cos \theta_r \theta_{\overline{x}}} = const_{,\tau}$$
 (2)

a simple relation can be derived for the irradiance and the radiance in that case because

$$\int L_{\text{PRD}} \cos \theta_{\text{r}} d\Omega = L_{\text{PRD}} \cdot \pi = \frac{\partial I}{\partial A} = E_{\text{i}} \qquad (3)$$

so that

$$L_{PRD} = \frac{1}{\pi} E_i, \tag{4}$$

Therefore the SRF and the BRDF differ only by a constant factor of  $\pi$ . The BRDF is more common than the SRF, especially in the realm of computer graphics. However, we use the latter in this paper because we feel that normalization to the perfectly reflecting diffusor diffusor is more intuitive and is the quantity in the calibration services provided by NMI.

Instruments that perform absolute measurements (PTB, CNAM, MSL and MIKES) do the normalization of the samples radiance to  $L_{\rm PRD}$  different than those that perform relative measurements. In the case of absolute measurements, the irradiance  $E_{\rm i}$  on the sample is acquired by measuring the radiance  $L_{\rm ii}$  of the light source. If  $\theta_{\rm ii}$  denotes the angle of incidence of the illumination on the sample and  $\omega\Omega_{\rm i} = A_{\rm i}/d^2$ , with the area  $A_{\rm i}$  of the light source and its distance d from the sample surface, is the solid angle of the illumination as viewed from the sample, then

$$L_{i} = E_{\overline{i}} \frac{E_{i}1}{\cos \theta_{i} \, \omega \Omega_{i}}. \tag{5}$$

#### **Deviation of KU Leuven**

